

Mark Scheme (Results)

January 2012

GCE Statistics S2 (6684) Paper 1

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General Marking Guidance

- All candidates must receive the same treatment. Examiners must mark the first candidate in exactly the same way as they mark the last.
- Mark schemes should be applied positively. Candidates must be rewarded for what they have shown they can do rather than penalised for omissions.
- Examiners should mark according to the mark scheme not according to their perception of where the grade boundaries may lie.
- There is no ceiling on achievement. All marks on the mark scheme should be used appropriately.
- All the marks on the mark scheme are designed to be awarded. Examiners should always award full marks if deserved, i.e. if the answer matches the mark scheme. Examiners should also be prepared to award zero marks if the candidate's response is not worthy of credit according to the mark scheme.
- Where some judgement is required, mark schemes will provide the principles by which marks will be awarded and exemplification may be limited.
- When examiners are in doubt regarding the application of the mark scheme to a candidate's response, the team leader must be consulted.
- Crossed out work should be marked UNLESS the candidate has replaced it with an alternative response.

EDEXCEL GCE MATHEMATICS

General Instructions for Marking

- 1. The total number of marks for the paper is 75.
- 2. The Edexcel Mathematics mark schemes use the following types of marks:
- M marks: method marks are awarded for 'knowing a method and attempting to apply it', unless otherwise indicated.
- A marks: Accuracy marks can only be awarded if the relevant method (M) marks have been earned.
- **B** marks are unconditional accuracy marks (independent of M marks)
- Marks should not be subdivided.
- 3. Abbreviations

These are some of the traditional marking abbreviations that will appear in the mark schemes and can be used if you are using the annotation facility on ePEN.

- bod benefit of doubt
- ft follow through
- the symbol / will be used for correct ft
- cao correct answer only
- cso correct solution only. There must be no errors in this part of the question to obtain this mark
- isw ignore subsequent working
- awrt answers which round to
- SC: special case
- oe or equivalent (and appropriate)
- dep dependent
- indep independent
- dp decimal places
- sf significant figures
- * The answer is printed on the paper
- 4. All A marks are 'correct answer only' (cao.), unless shown, for example, as A1 ft to indicate that previous wrong working is to be followed through. After a misread however, the subsequent A marks affected are treated as A ft, but manifestly absurd answers should never be awarded A marks.

General Principals for Core Mathematics Marking

(But note that specific mark schemes may sometimes override these general principles).

Method mark for solving 3 term quadratic:

1. Factorisation

$$(x^2 + bx + c) = (x + p)(x + q), \text{ where } |pq| = |c|, \text{ leading to } x = \dots$$

$$(ax^2 + bx + c) = (mx + p)(nx + q), \text{ where } |pq| = |c| \text{ and } |mn| = |a|, \text{ leading to } x = \dots$$

2. Formula

Attempt to use <u>correct</u> formula (with values for a, b and c), leading to x = ...

3. Completing the square

Solving
$$x^2 + bx + c = 0$$
: $\left(x \pm \frac{b}{2}\right)^2 \pm q \pm c, \quad q \neq 0$, leading to $x = \dots$

Method marks for differentiation and integration:

Differentiation

Power of at least one term decreased by 1. $(x^n \rightarrow x^{n-1})$

2. Integration

Power of at least one term increased by 1. ($x^n \rightarrow x^{n+1}$)

Use of a formula

Where a method involves using a formula that has been learnt, the advice given in recent examiners' reports is that the formula should be quoted first.

Normal marking procedure is as follows:

<u>Method mark</u> for quoting a correct formula and attempting to use it, even if there are mistakes in the substitution of values.

Where the formula is <u>not</u> quoted, the method mark can be gained by implication from <u>correct</u> working with values, but may be lost if there is any mistake in the working.

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Question Number	Scheme	Mark	S
1 (a)	$E(X) = \frac{9+3}{2} = 6$	B1	(1)
(b)	$Var(X) = \frac{(9-3)^2}{12} = 3$	M1A1	(2)
(c)	$P(X > 7) = (9-7) \times \frac{1}{6} = \frac{1}{3}$	M1A1	
(d)	$P(X < 6 X > 4) = \frac{P(4 < X < 6)}{P(X > 4)}$	M1A1	(2)
	$=\frac{\frac{2}{6}}{\frac{5}{6}}=\frac{2}{5}$	A1	
	$\frac{3}{6}$		(3) 8
	Notes		
(b)	M1 $\frac{(9-3)^2}{12}$ or $\frac{(9+3)^2}{12}$		
(c)	M1 $\frac{(9-7)}{6}$ or $1 - \frac{(7-3)}{6}$ or $\int_{7}^{9} \frac{1}{6} dx$ or $1 - \int_{3}^{7} \frac{1}{6} dx$		
	A1 Also acceptable 0.3, 0.33 and awrt 0.333		
(d)	M1 $\frac{P(4 < X < 6)}{P(X > 4)}$ or $\frac{P(X < 6)}{P(X > 4)}$ or $\frac{\frac{2}{6}}{\frac{5}{6}}$ or $\frac{\frac{3}{6}}{\frac{5}{6}}$ or $1 - \frac{P(X > 6)}{P(X > 4)}$ or $\frac{6 - 4}{9 - 4}$ or $\frac{3}{5}$		
	A1 $\frac{P(4 < X < 6)}{P(X > 4)}$ or $\frac{\frac{2}{6}}{\frac{5}{6}}$ or $1 - \frac{P(X > 6)}{P(X > 4)}$ or $\frac{6 - 4}{9 - 4}$		
	An answer of $\frac{2}{5}$ gains all 3 marks.		
	$NB \le and \ge are accepted in the above formulae$		

Question Number	Scheme		Marks
2	$H_0: p = 0.5$ $H_1: p > 0.5$	B1 B1	
	1 -	correct Bin M	
	$P(X \ge 21) = 1 - P(X \le 20)$ or $P(X \le 19) = 0.9506$ $P(X \ge 20) = 0.0494$	M	1
	$= 0.0214$ CR $X \ge 20$	A1	
	so significant/reject H ₀ /in Critical region	M	1 dep
	Evidence to suggest <u>David's claim is incorrect</u> or The weather <u>forecast</u> produced by the local <u>radio</u> is better than those at <u>tossing/flipping a coin</u>	chieved by A1	(7) 7
	Notes	J	

Notes

 $1^{\text{st}} B1 \text{ for } H_0: p = 0.5$

 2^{nd} B1 for $H_1: p > 0.5$

SC If both hypotheses are correct but a different letter to *p* is used they get B1 B0. If no letter is used they get B0 B0.

1st M1 writing or using B(30,0.5)

One tail

 2^{nd} M1 for writing or using 1 - P($X \le 20$) or writing P($X \le 19$) = 0.9506 or P($X \ge 20$) = 0.0494. May be implied by correct CR.or probability = 0.0214

A1 for 0.0214 or CR $X \ge 20/X > 19$. **NB** $P(X \le 20) = 0.9786$ on its own scores M1A1

 3^{rd} M1 dependent on the 2^{nd} M1 being awarded. For a correct statement based on the table below. Do not allow non-contextual conflicting statements eg "significant" and "accept H_0 ". **Ignore comparisons**.

2nd A1 for a correct contextualised statement. NB A correct contextual statement on its own scores M1A1.

	0.05	p < 0.05 or p > 0.95
3 rd M1	not significant/ accept H ₀ / Not in CR	significant/ reject H ₀ / In CR
2 nd A1	David's claim is correct	David's claim incorrect
	weather forecast produced by the local radio is	weather forecast produced by the local radio is
	no better than those achieved by	better than those achieved by tossing/flipping a
	tossing/flipping a coin	<u>coin</u>

Two tail

1st M1 for writing or using 1 - $P(X \le 20)$ or writing $P(X \le 20) = 0.9786$ or $P(X \ge 21) = 0.0214$. May be implied by correct CR. or probability = 0.197

A1 for 0.0214 or CR $X \ge 21/X > 20$. **NB** $P(X \le 20) = 0.9786$ on its own scores M1A1

 3^{rd} M1 dependent on the 2^{nd} M1 being awarded . For a correct statement based on the table below. Do not allow non-contextual conflicting statements eg"significant" and "accept H_0 " . **Ignore comparisons**.

 2^{nd} A1 for a correct contextualised statement. NB A correct contextual statement on its own scores M1A1.

	0.025	p < 0.025 or p > 0.975
3 rd M1	not significant/ accept H ₀ / Not in CR	significant/ reject H ₀ / In CR
2 nd A1	David's .claim is correct weather <u>forecast</u> produced by the local <u>radio</u> is no better than those achieved by tossing/flipping a coin	David's claim incorrect weather <u>forecast</u> produced by the local <u>radio</u> is better than those achieved by tossing/flipping a coin

Question	Scheme	Marks	
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Number			
3 (a)	$P(X = 0) = 0.85^{10}$ or from tables	M1	
	= 0.1969 awrt 0.197	A1	
(b)	$P(X > 3) = 1 - P(X \le 3)$	M1	(2)
	=1-0.6477 = 0.3523 awrt 0.352	A1	(2)
(c)	$n \times 0.15 = 5$	M1	(2)
	n = 33 or 34	A1	(2)
(d)	1 - P(X = 0) > 0.95	M1 A1	(-)
	$1 - (0.85)^n > 0.95.$ $0.85^n < 0.05$	AI	
	n > 18.4 $n = 19$	A1	
	n-1	AI	(3) 9
	Notes		
(a)	M1 $(p)^{10}$ with 0		
(b)	M1writing or using 1 - P($X \le 3$)		
(c)	M1 $np = 5$ 0		
(d)	M1 writing or using $1 - P(X = 0) > 0.95$ or $P(X = 0) < 0.05$ (also accepted are $= \text{ or } \ge \text{ in }$ and $= \text{ or } \le \text{ instead of or } <)$ $P(X \le 0)$ is equivalent to $P(X = 0)$ A1 writing or using $1 - (0.85)^n > 0.95$ or $(0.85)^n < 0.05$ (also accepted are $\ge \text{ instead of or } <$). Any value of n may be used A1 cao		
	NB an answer of 18.4 gets M1 A1 A0		
	An answer of 19 gets M1 A1 A1 unless it follows from clearly incorrect working.		
		<u> </u>	

Question Number	Scheme	Mark	S
4 (a)	Poisson	B1	(1)
(b)	Hits occur singly in time Hits are independent <u>or</u> Hits occur randomly Hits occur at a constant rate	B1B1	(2)
(c)	<i>X</i> ~ Po(5)	B1	
	$P(X = 10) = P(X \le 10) - P(X \le 9)$ or $\frac{e^{-5} 5^{10}}{10!}$	M1	
	= 0.9863 - 0.9682 = 0.0181 awrt 0.0181	A1	(3)
(d)	<i>X</i> ∼ Po(10)	B1	(3)
	$P(X \ge 15) = 1 - P(X \le 14)$	M1	
	= 1 - 0.9165 = 0.0835 awrt 0 .0835	A1	(3)
(e)	X~ Po(50) Approximated by N(50,50)	B1B1	, ,
	$P(X > 70) = P\left(Z > \frac{70.5 - 50}{\sqrt{50}}\right)$	M1M1	
	= P(Z > 2.899)	A1	
	=1-0.9981	M1	
	= 0.0019 awrt 0.0019	A1	
			(7) 16
(b) (c)	Notes 1st B1 Any one of the 3 statements - no context required. NB It must be a constant (mean) rate constant probability or a constant mean. 2nd B1 A different statement with context of <u>hits.</u> NB random and independent are the same statement or using Po(5) $e^{-5}5^{10}$		
	M1 writing or using $P(X \le 10) - P(X \le 9)$ or $\frac{e^{-5} 5^{10}}{10!}$		
(d)	B1 writing or using Po(10) M1 writing or using 1- $P(X \le 14)$		
(e)	1st B1 for a normal approximation 2nd B1 for correct mean and sd (may be seen in standardis 1st M1 for attempting a continuity correction (71 ± 0.5) 2nd M1 Standardising using their mean and their sd and using [69.5, 70, 70.5, 71 or 71.5] allow NB if they have not written down a mean and sd then they need to be correct in the standardisa this mark.	$w \pm z$	
	1st A1 for $z = \pm$ awrt 2.9 or better. May be awarded for $\pm \frac{70.5 - 50}{\sqrt{50}}$		
	3rd M1 for 1 - tables value		
	SC using P(X< 70.5/71.5) – P(X<69.5/70.5) can get B1B1 M0M1A0 M0A0		

Question Number	Scheme	Mark	5
5 (a)	$X \sim B(120, 0.075)$	B1	
	Approximated by Po(9) $P(X > 3) = 1 - P(X \le 3)$	M1A1 M1	
	= 1 - 0.0212 = 0.9788 awrt 0.979	A1	(5)
(b)	P(At least 4 defective components in each box) = $P(X>3)\times P(X>3)$	M1	
	$= 0.9788^{2}$ $= 0.95804944$ awrt 0.958	A1	(2)
(a)	Notes B1 Writing or use of B(120,0.075) may be implied by using Po(9) or N(9,8.325) 1st M1 writing or use of Poisson 1st A1 writing or use of Po(9) 2nd M1 for writing or using 1- P($X \le 3$) or this may be implied by an awrt 0.972 using normal approximation.		
(b)	M1 ((their (a)) 2 or 0.979^2 or 0.9788^2 or 0.98^2		

Question Number	Scheme	Marks
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		1
6 (a)	f(x)	
	k-0.5	D1
	shape labels	B1 B1
	0.5	
	0 1 k x	(2)
(1-)	$\binom{k}{1}\binom{n}{n}$	
(b)	$\int_{1}^{1} \left(x - \frac{1}{2}\right) dx = \frac{1}{2}$	M1
	$\int_{1}^{k} \left(x - \frac{1}{2} \right) dx = \frac{1}{2}$ $\left[\frac{1}{2} x^{2} - \frac{1}{2} x \right]_{1}^{k} = \frac{1}{2}$ $k^{2} - k - 1 = 0 \text{o.e.}$ $k = \frac{1}{2} \left(1 + \sqrt{5} \right)$	
	$\begin{bmatrix} 2^{x} & 2^{x} \end{bmatrix}_{1}^{2} = 2$ $\begin{bmatrix} k^{2} & k & 1 = 0 \\ 0 & 0 & 0 \end{bmatrix}$	A1
	$k = \frac{1}{1}(1 + \sqrt{5})$	M1A1 cso
	2(1.40)	(4)
(c)		
	$\left \frac{1}{2}x, \right 0 \le x < 1$	B1
	$F(x) = \begin{cases} 0, & x < 0 \\ \frac{1}{2}x, & 0 \le x < 1 \\ \frac{1}{2}x^2 - \frac{1}{2}x + \frac{1}{2}, 1 \le x \le k \\ 1, & x > k \end{cases}$	M1A1A1B1
	$\begin{vmatrix} 2 & 2 & 2 \\ 1, & x > k \end{vmatrix}$	B1 1st and last
	Note: Working for the M1A1A1	(6)
	$\int_{1}^{k} x - \frac{1}{2} dx + C = \frac{1}{2} x^{2} - \frac{1}{2} x ; + \frac{1}{2}$	(M1A1;A1)
(d)	P(0.5 < X < 1.5) = F(1.5) - F(0.5)	
	= 0.875 - 0.25 = 0.625	M1 A1
		(2)
(e)	Median is $x = 1$	B1
	Mode is $x = k$ or $\frac{1}{2}(1+\sqrt{5})$ or awrt1.62	B1 (2)
(f)	Negative skew	B1
	Median <mode are="" from="" graph="" more="" or="" right.<="" th="" the="" to="" values=""><th>B1d (2)</th></mode>	B1d (2)
	No.	18
(a)	Notes 1st B1 Correct shape with straight lines. Must all be above the <i>x</i> -axis	
	2nd B1 A fully correct graph with the labels 1, k , 0.5, k - 0.5 seen in the correct places. Allow the use of $\frac{1}{2}(1+\sqrt{5})$ /awrt 1.62 instead of k .	
	2 1 1 V 5)/ awit 1.02 instead of k.	

	1	
(b)	1st M1 $\int_{1}^{k} x - \frac{1}{2} dx = 0.5$	
	or $\int_{1}^{k} x - \frac{1}{2} dx + 0.5 = 1$ ignore limits	
	or $\int_{1}^{k} x - \frac{1}{2} dx + \int_{1}^{k} \frac{1}{2} dx = 1$	
	or $\frac{1}{2}(k-0.5+0.5)(k-1) = 0.5$ or any correct method of finding the area	
	1st A1 for a quadratic equation in the form $a(k^2 - k - 1) = 0$ or $ak^2 - ak = a$. where a is a 2^{nd} M1 correct method for solving a quadratic of the form $ak^2 - bk + c = 0$ where a,b,c must be at least one correct step before the final answer. Allow substituting in k into a the form $ak^2 - bk + c = 0$.	$\neq 0$. There
	$2^{\text{nd}} \text{ A1 } \text{ cso for } k = \frac{1}{2} (1 + \sqrt{5})$	
(c)	1st B1 for second line. Do not penalise the use of $<$ instead of \le and vice versa	
	M1 for use of $\int_1^k x - \frac{1}{2} dx + C$ ignore limits. For use they must have $x \to x^2$	
	1st A1 correct integration $\frac{1}{2}x^2 - \frac{1}{2}x$	
	2nd A1 C = $\frac{1}{2}$	
	NB M1A1A1 may be implied by correct 3rd line in $F(x)$	
	2nd B1 for 3rd line. Statement of the form $\frac{1}{2}x^2 - \frac{1}{2}x \pm C$. Do not penalise the use of < inste	ad of \leq and
	vice versa. Allow k or value of k. C may equal 0.	
	3rd B1 for first and last line. Do not penalise the use of \leq instead of $<$ and \geq instead of $>$. Allow k or value of k	
(d)	M1 <u>Using</u> $F(1.5) - F(0.5)$. 1.5 must be put into the third line of the c.d.f. and 0.5 must be put into the second line of the c.d.f	
	or $\int_{0.5}^{1} \frac{1}{2} x dx + \int_{1}^{1.5} x - \frac{1}{2} dx$ need to attempt integration, at least one $x^n \rightarrow x^{n+1}$	
	or seeing $0.25 + 0.375$ or any correct method of finding the area (NB if they have not used + C or C = 0 they will get 0.125. This will get M1A0). An answer	
(e)	of 0.125 from an incorrect method gains M0 A0. If it is not clear which one is the mode and which one is the median assume the median is the first answer and mode the second.	
(f)	B1 negative/negative skew(ness). Do not allow negative correlation. B1 dependent on previous B mark being awarded. Reason must follow from their values or diagram.	

Question Number	Scheme	Marks	
7 (a) (i)	The <u>range of values/region/area/set of values</u> of the test statistic that would lead you	B1	
	to <u>reject H</u> ₀		
(a) (ii)	The probability of incorrectly rejecting H ₀ or	B1	
	Probability of rejecting H_0 when H_0 is true	(2	()

(b) (i)	$X \sim Po(8)$				M1		
	$P(X \le 4) = 0.0996$						
	$P(X \le 3) = 0.0424$						
	` ′	Critical region [0,3]					
(b) (ii)	awrt 0.0424				B1	(3)	
(c)	$H_0: \lambda = 8 (\text{or } \mu = 8)$				B1		
		8 $(\text{or }\mu > 8)$					
	$P(X \ge 13) = 1 - P(X \le 12)$,	or $P(X \le 13) = 0.9658$ or $P(X \ge 14) = 0.0342$			
	= 1 - 0.9362						
		= 0.0638	$CR X \ge 14$		A1		
	so insufficient evidence to reject H_0 /not significant/ not in critical region				M1 dep		
	There in insufficient evidence of an increase/change in the rate/number of sales per				A1		
	month <u>or</u> the estate <u>agents</u> claim is incorrect					(5)	
Notes						10	
(a)(i)	Allow accept H ₁ instead of reject H ₀ . It must be clear which hypothesis gets rejected/accepted.						
(ii)	Allow equivalent wording.						
(b)	M1 Writing or using Po(8). May be implied by correct critical region.						
	A1 allow 0	A1 allow $0 \le X \le 3$ or $CR \le 3$ or $X \le 3$. Any letter may be used but not $P(X \le 3)$. This must be on its own.					
(c)	B1 both hy	B1 both hypotheses correct. Must use λ or μ .					
	One tail 1 st M1 for writing or using 1 - P($X \le 12$) or writing P($X \le 13$) = 0.9658 or P($X \ge 14$) = 0.0342. May be implied by correct CR.or probability = 0.0638 A1 for 0.0638 or $X \ge 14$. Allow $X > 13$. NB P($X \le 12$) = 0.9362 on its own scores M1A1 2 nd M1 dependent on the 1 st M1 being awarded. For a correct statement based on the table below. Do not allow no contextual conflicting statements eg "not significant" and "reject H ₀ ". Ignore comparisons.						
			palised statement. NB A correct contextual statement on its own scores M1A1.				
	and a se	0.05		p < 0.05 or p > 0.95			
	2 nd M1 not significant/ accept H ₀ / Not in CR significant/ reject H ₀ / In CR 2 nd A1 Insufficient evidence of an increase/change in the Sufficient evidence of an increase/				ange in the	_	
	rate/number of sales per month rate/number of sales per month				ange in the		
	Two tail						
	1 st M1 for writing or using 1 - $P(X \le 12)$ or writing $P(X \le 14) = 0.9827$ or $P(X \ge 15) = 0.0173$. May be implied by correct CR.or probability = 0.0638						
	A1 for 0.0638 or $X \ge 15$. Allow $X > 14$. NB P($X \le 12$) = 0.9362 on its own scores M1A1						
	2 nd M1 dependent on the 1 st M1 being awarded. For a correct statement based on the table below. Do not allow non-						
	contextual conflicting statements eg "not significant" and "reject H_0 ". Ignore comparisons. $ 2^{\text{nd}} \text{ A1 for a correct contextualised statement. NB A correct contextual statement on its own scores M1A1.} $ $ 0.025 p < 0.025 \text{ or } p > 0.975 $						
						1	
	2 nd M1	not significant/ accept H ₀ /		significant/ reject H ₀ / In CR			
	2 nd A1	2 nd A1 Insufficient evidence of an increase/change in the rate/number of sales per month Sufficient evidence of an increase/change in the rate/number of sales per month			nge in the		

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